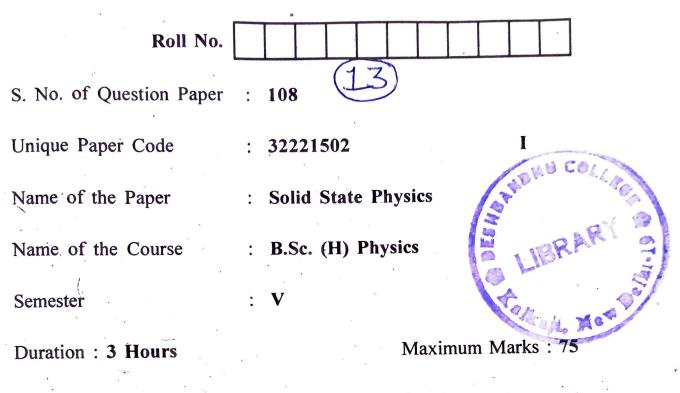
12/12/18





(Write your Roll No. on the top immediately on receipt of this question paper.)

Attempt any five questions. Question No. 1 is compulsory.

All questions carry equal marks.

1. Attempt any *five* of the following

5×3=15

(*a*) Draw P-E hysteresis loop for a ferroelectric material. Write mathematical statement of Curie-Weiss law for ferroelectric materials.

(b) Differentiate between acoustical and optical phonons.

- (c) Explain the formation of cooper pair in superconductors.
- (d) Write the primitive translational vectors of hexagonal lattice.

P.T.O.

- (e) Show that every reciprocal lattice vector  $\vec{G}_{hkl}$  is normal to the plane  $(h \ k \ l)$ .
- (f) Calculate the Hall coefficient of Na based on free electron model. Na has b.c.c structure and side of the cube is 4.28 Å.
- (g) Draw the variation of total polarizability with frequency of external electric field.
- (h) What is the difference between Phonon and Plasmon ?
- (a) Derive Bragg's law in the reciprocal lattice. 8

2.

- (b) In a simple cubic crystal, show that the first order reflection from (n00) planes is equivalent (mathematically) to the *n*th order reflection from (100) plane ?
- (a) Derive an expression for the specific heat of a solid on .
   the Debye model and show that, at low temperature, it follows T<sup>3</sup>-law.
  - (b) Derive the dispersion relation for a linear monoatomic lattice and show that the group velocity and phase velocity of a wave are equal in the long wavelength limit.
- (a) Show that the classical paramagnetic susceptibility is given by  $\chi = \frac{\mu_0 N}{3kT} \mu^2$ , where symbols have their usual meanings.

- (b) How was the classical Langevin's theory of paramagnetism modified by Weiss ?
   5
- (a) Derive an expression for the electronic polarizability in a time varying electric field, and hence derive the Cauchy and Sellmeir relations.
- (b) Distinguish between normal and anomalous dispersion ? 3
- 6. (a) Explain the formation of allowed and forbidden energy bands for the motion of an electron in one-dimensional periodic potential in solids.
  - (b) Prove that effective mass of electron is given by  $m^* = \hbar^2 / (d^2 E / d^2 k).$  5
- 7. (a) Explain how the Meissner-effect was explained by London. 6
  - (b) What is Isotope effect ? 3
  - (c) What do you understand by Piezoelectric effect,
     Pyroelectric effect & Electrostrictive effect ? 6
- 8. (a) Prove that reciprocal lattice of bcc is fcc and that of fcc is bcc. 10

(b) Show that five-fold rotational symmetry does not exist?

5

108

108

5.

3

2,100

S. No. of Question paper	: 1656
Unique Paper Code	: 222501 (14)
Name of the Paper	: Mathematical Physics V
Name of the Course	: B.Sc. (Hons.) Physics
Semester	: V



Duration: 3 Hours

Maximum marks: 75

(Write your Roll No. on the top immediately on receipt of this question paper.)

Attempt *five* questions in all. Question number 1 is compulsory.

Do two questions from each section

- 1. Attempt any *five* of the following:
  - (a) Find Fourier Sine Transform of  $\frac{1}{x}$ .
  - (b) If F(s) is the Fourier transform of f(x), find the Fourier transform of  $F[x^n f(x)]$
  - (c) If  $L{f(t)}$  is F(s) then find  $L{t^n}$ .
  - (d) Find  $L\{\cos(at)\}$ .
  - (e) Show that  $\delta(\alpha x) = \frac{\delta(x)}{|\alpha|}$ , where  $\alpha > 0$ .
  - (f) Define contravariant and covariant tensors.
  - (g) Find Laplace transform of  $t^2u(t-3)$ .

## $3 \times 5 = 15$

10,5

## Section - A

2.

3.

6

(a) Find Fourier Sine transform of  $f(x) = e^{-\beta x}$  ( $\beta > 0$ ) and hence show that

$$\frac{\pi}{2} e^{-\beta x} = \int_0^\infty \frac{\lambda \sin(\lambda x)}{\beta^2 + \lambda^2}$$

- (b) Find Fourier Cosine transform of  $x^{n-1}$ .
- (a) State the convolution theorem for Laplace transform and use it to evaluate the inverse Laplace transform of  $\frac{2}{s(s^2+16)}$

(a) Solve the following differential equations using Laplace transform. dx

$$\frac{dt}{dt} + y = 0; \ \frac{dy}{dt} - x = 0; \ x(0) = 1 \ ; y(0) = 1$$
 8,7

(a) Show that the Laplace transform of a periodic function f(t) is

 $\frac{\int_0^T f(t)e^{-st}dt}{1-e^{-sT}} \quad \text{, where } \mathbf{f}(t+T) = \mathbf{f}(t), s > 0$ 

(b) Find Laplace transform of f(t) where:

$$f(t) = \begin{cases} t & 0 < t \le c \\ 2c - t & c < t < 2c \end{cases}$$
8,7

## Section B

- (a) State and prove initial value theorem in Laplace transform.
- (b) Solve the following differential equation using Laplace transform

 $y'' + 2y' + 5y = e^{-x}Sin(x);$  y(0) = 0, y'(0) = 1 with y'' and y' as the second and first derivative of y(x) respectively.

5,10

6. (a) Prove the identity

 $\nabla . (A X B) = B . (\nabla X A) - A . (\nabla X B)$ 

- (b) State and Prove quotient law in tensors.
- (c) Show that every second order tensor can be expressed as the sum of two tensors, one of which is symmetric and other skew symmetric.

5,5,5

- (a) Derive an expression for the moment of inertia tensor. Prove that it is a symmetric tensor and it transforms like a second order tensor.
  - (b) Show that:

 $\epsilon_{iks} \; \epsilon_{mps} = \delta_{im} \, \delta_{kp} - \delta_{ip} \, \delta_{km}$ 

10, 5

4.

5.

7.